

## Utility Maximization with Perfect Substitutes 2

Consider a consumer who views two goods  $x_1$  and  $x_2$  as perfect substitutes. The consumer regards one unit of  $x_1$  as equivalent to two units of  $x_2$ . The prices are given by  $p_1 = 8$  and  $p_2 = 3$  and the income is  $M = 100$ .

## Solution

Since the goods are perfect substitutes the indifference curves are linear with a constant slope. Given that one unit of  $x_1$  is equivalent to two units of  $x_2$  the slope of the indifference curve is

$$MRS = 2$$

The slope of the budget line is determined by the price ratio

$$Slope_{budget} = \frac{p_1}{p_2} = \frac{8}{3}$$

Comparing the slopes we note that

$$MRS < Slope_{budget}$$

This implies that the consumer obtains more utility per unit cost from  $x_2$  than from  $x_1$  and will therefore spend the entire income on  $x_2$ .

Thus the optimal consumption bundle is

$$x_1^* = 0$$

$$x_2^* = \frac{M}{p_2} = \frac{100}{3}$$